# APPLICATION OF PRINCIPAL COMPONENT ANALYSIS TO CLASSIFY NORMAL BRAIN TISSUE AND BRAIN LESIONS LIKE LOW AND HIGH GRADE GLIOMA, METASTASES AND MULTIPLE SCLEROSIS 

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#### Abstract

Principal Component Analysis ( PCA) an extremely useful method of Statistical techniques is applied when working with a lot of parameters or independent numerical variables to predict the different pathological lesions in the brain like Multiple Sclerosis (MS), Glioma, Glioblastoma of different grades and Metastasis. Statistical techniques such as factor analysis or Principal Component Analysis(PCA) help to overcome such difficulties.

In different brain diseases structural alterations in the normal tissue may be noticed in $M R$ images. It is not so simple to detect the brain lesions correctly even from the MR spectroscopic graph. Enormous data collected from various patients such as - Refractive Index, T2 relaxation values, Apparent Diffusion Coefficient (ADC), Creatine (CR), Choline (CHO), NAA (N-Acetyl Aspartate), ratio of CR/NAA, LIP/LAC (Lipid/lactate), MI ( Myoinositol), CHO/CR and T2 value in the periphery of lesion may be confusing. The relationship between each variable may not be clear and that there is a chance of over fitting the data. By reducing the dimension of the feature space by "feature elimination" and "feature extraction", there may be less chance of over fitting the data. PCA helps identifying the disease condition in doubtful cases by generating a map depicting and classifying the diseases.


Keywords: Principal Component Analysis (PCA); Magnetic Resonance Imaging (MRI); Metabolites of MR Spectroscopy; Refractive Index (RI); Ground Truth Image: Independent Numeric and Dependent Variable ; Prediction.

## INTRODUCTION:

Tissue characterization or accurate diagnosis is not possible by observing the structural changes in the MR images without getting the histopathologial study after a brain biopsy (Figure1) [1,2]. Sometimes some confusion is created by the images of Glioma in different stages, Glioblastoma, metastasis from primary cancer site and benign diseases like multiple sclerosis (relapsing remitting or tumefactive multiple sclerosis) [2]. Even MR Spectroscopy (MRS) fails to detect the exact character of the lesion from the graph generated by the peak of different metabolites along with the quantity [3, 4]. In this study, Principal component Analysis (PCA) had been tried to simplify the physical and chemical data derived from the MR Images [5]. PCA is a sophisticated and extensively used procedure for deciding the composition of recurrent variability.

One of the important problems in MR image processing is classification of diseases and tissue character based on chemical and physical information. Depending on attributes of multiple independent numeric variables extracted from the input images or ground truth images prediction of disease/tissue classification can be made by PCA [6].


Figure1 A. Glioblastoma B. Multiple Sclerosis (MS), C. MRS-showing metabolites D. Arachnoid Cyst. E. T2 map F. ADC MAP

This classification process of PCA relies on two steps:

1) At first step the classifier model is built to discern the predefined group of the image classes [5,6]. The classifier model is created based on a data structure consisting of multiple parts like Independent Numeric Variable of different parameters and Dependent variable of diagnosis of diseases or tissues.
2) Second step: The constructed classifier model is used to classify diseases [6].

## PRINCIPAL COMPONENT ANALYSIS (PCA)

For data analysis, multiple components or inputs as independent variables were tabulated. Out of them each component is a vector comprising of principal component score derived from each predictor variable of output. The data set may have many variables (31 rows and 12columns) and most of the variables are correlated. Some strategic method or technique to be adopted to reduce the number of variables and to retain some important variables [7].

This PCA technique has the ability to minimize the dimension of the data set in such a way that it becomes effortless to analyze, visualize and interpret. Prediction of the tissue and diseases is also plausible by a statistical procedure that transforms a set of correlated variables or observations into a lesser number of uncorrelated variables of principal components [8].
PCA helps in data compression by Feature eliminating and Feature Extraction. The purpose of this method is to diminish dimension of the variables which may not be required for interpretation [9].

## Back ground of PCA:

For pattern recognition in the data containing maximum dimension which are identical or dissimilar, PCA has a role to analyze the data set [10]. In images of face recognition and image compression PCA is widely used.

From the different variables, PCA finds a linear combination such that the maximum difference or variance is identified from the variables. During feature eliminating process from the variables there may be a chance of missing the dropped variables which could contribute or could have produced benefit to the prediction [10,11]. In feature extraction, if there is a particular number of independent variables then same number of new independent variables are created and each new independent variable becomes an amalgamation of each of the previously
used "old" independent variables. However, these new independent variables are created in a special order or specific way to predict the dependent variable [10-12].

As an extra benefit, each of the new variables after PCA may be all independent of one another. This is an advantage to fit a linear regression model with these new variables. The spread of the data set has different measure or "Variance" [13,14]. In fact it is almost identical to the standard deviation [14].

The formula of variance is depicted here [14]:

$$
s^{2}=\frac{\sum_{i=1}^{n}\left(X_{i}-\bar{X}\right)^{2}}{(n-1)}
$$

This variance is then eliminated and PCA searches for a second linear combination which usually gives details of the greatest magnitude of the remaining variance, and this process repeats almost immediately. PCA is very much significant if there is a data set of a large number of variables with some redundancy in these variables that means some of the variables are correlated with one another [15]. So, a smaller number of principal components (artificial variables) are generated by shrinkage or reducing the observed variables of most of the variance in the observed variables [15].

Multivariate data works with the interaction between numerous random variables. The sets of observations of the random variables are represented by a multivariate data matrix .

Variance is an important parameter to measure spread of data of observed values. It is the range to which an allocation is stretched or compressed[16].

The amount of variance is measured by Eigenvalues or the Characteristic roots which explain a given factor or feature measuring a variance or difference of the total sample [16]. Eigenvalues or vectors are characteristic of a matrix. The principal components are orthogonal or right angled to one another, and they are statistically independent of one another [16].

## METHODS:

## Data collection :

After getting institutional ethics 131 patients of different gender and age (from 9 to 84 years) were studied in a 3 Tesla MR Magnet (SIGNA HDxt, GE, USA). Histo-pathological diagnosis of the materials collected from the Stereotaxic and post surgery biopsies were made and correlated with the following parameters [17-19] :

## PARAMETERS

RI VALUES: RI of tissues collected from biopsies of brain materials were determined by Abbe Refractometer (Suprashes Model AAR-33, India) [17-19].

T2 RELAXATION VALUES: T2 mapping was done with the help of multi ECHO read out train (with different echo times $30,60,90,120,150,180 \mathrm{~ms}$ respectively) in the 3 T MR, with a TR of 4000 ms . T2 relaxation value of various brain tissue and brain lesions were generated from the map [17]
( Figure1E).

ADC (APPARENT DIFFUSION COEFFICIENT): ADC map was created in the MR magnet and ADC values of the tissues were determined depicting rate of diffusion of water within the tissues $\mathrm{mm}^{2} / \mathrm{sec}($ Figure 1F).

METABOLITES QUANTIFICATION OF MR SPECTROSCOPY (MRS): By single and multi voxel Spectroscopy applying PRESS technique, TR- 9602 and TE- 35-144ms quantification of metabolites like CHO,CR,NAA,MI, Lipid, Lactate, CHO NAA,CHO CR and CHO NAA ratio was determined [17-20] (Figure1c).

GROUND TRUTH MR INPUT IMAGE: Therefore a ground truth MR image thus formed, consists of information like RI values (derived from RI mapping), T2 values (from T2 mapping) and ADC values (from ADC mapping) and metabolites from the MRS quantification.All the data were tabulated in Table1 [17].

TABLE 1. Showing all the data collected from the patients and MR magnet:

| DISEASE | RI | T2 | CHO | ADC | CR | CR/NAA | LIP/LAC | MI | $\mathrm{CH} / \mathrm{CR}$ | T2peri | CHO/NAA |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| CSF | 1.3333 | 400 | 1610 | 300 | 1400 | 0.346 | 1400 | 910 | 1.15 | 400 | 0.402 |
| CSF | 1.3334 | 395 | 1680 | 320 | 1800 | 0.367 | 1760 | 1056 | 1.14 | 395 | 0.412 |
| CSF | 1.3335 | 390 | 1700 | 330 | 1967 | 0.389 | 1600 | 1076 | 1.15 | 390 | 0.432 |
| CSF | 1.3336 | 384 | 1890 | 340 | 1989 | 0.411 | 1675 | 1080 | 1.14 | 384 | 0.498 |
| ms | 1.3421 | 340 | 11750 | 145 | 8320 | 0.557 | 4160 | 2912 | 1.4 | 240 | 0.779 |
| ms | 1.3439 | 328 | 8904 | 135 | 2800 | 0.433 | 4490 | 5576 | 3.15 | 241 | 1.39 |
| ms | 1.3498 | 316 | 7896 | 124 | 4560 | 0.225 | 3570 | 3536 | 1.73 | 243 | 0.389 |
| ms | 1.3497 | 304 | 5947 | 120 | 5400 | 0.7396 | 6766 | 4294 | 1.1 | 245 | 0.873 |
| ms | 1.3589 | 249 | 3448 | 75 | 3320 | 0.7112 | 5423 | 2322 | 1.02 | 230 | 0.821 |
| ms | 1.3641 | 245 | 1610 | 73 | 2212 | 0.941 | 1440 | 364 | 0.495 | 227 | 0.465 |
| gmatter | 1.3956 | 130 | 1601 | 76 | 2209 | 0.938 | 1441 | 362 | 0.491 | 166 | 0.461 |
| gmatter | 1.3956 | 125 | 1601 | 76 | 2209 | 0.938 | 1441 | 362 | 0.491 | 168 | 0.461 |
| gmatter | 1.3957 | 123 | 1589 | 78 | 2219 | 0.941 | 1467 | 345 | 0.491 | 167 | 0.459 |
| gmatter | 1.3952 | 121 | 1458 | 80 | 2320 | 0.878 | 1443 | 321 | 0.494 | 169 | 0.456 |
| w matter | 1.4251 | 95 | 1180 | 70 | 2443 | 0.788 | 1345 | 312 | 0.488 | 148 | 0.453 |
| w matter | 1.4256 | 89 | 1108 | 71 | 2435 | 0.771 | 1341 | 320 | 0.468 | 146 | 0.447 |
| w matter | 1.4259 | 85 | 1098 | 77 | 2387 | 0.774 | 1211 | 321 | 0.467 | 150 | 0.445 |
| edema | 1.3741 | 160 | 1231 | 84 | 2216 | 0.776 | 1123 | 325 | 0.467 | 246 | 0.443 |
| edema | 1.3823 | 182 | 1331 | 130 | 2321 | 0.787 | 1011 | 321 | 0.456 | 243 | 0.442 |
| edema | 1.3821 | 182 | 1298 | 128 | 2314 | 0.781 | 1009 | 314 | 0.454 | 244 | 0.441 |
| edema | 1.3822 | 184 | 1444 | 131 | 2310 | 0.778 | 1001 | 313 | 0.445 | 245 | 0.441 |
| GLIOMA | 1.4331 | 90 | 1443 | 127 | 2243 | 0.766 | 989 | 310 | 0.423 | 175 | 0.431 |
| GLIOMA | 1.4446 | 99 | 1365 | 177 | 2254 | 0.712 | 917 | 300 | 0.343 | 170 | 0.341 |
| Gblastma | 1.4551 | 110 | 2655 | 156 | 2112 | 0.678 | 900 | 311 | 0.311 | 195 | 0.332 |
| Gblastma | 1.4512 | 116 | 2774 | 142 | 3280 | 1.06 | 2240 | 312 | 0.844 | 190 | 0.907 |
| Gblastma | 1.4562 | 118 | 2661 | 140 | 3189 | 1.02 | 2134 | 314 | 0.7881 | 185 | 0.89 |
| Gblastma | 1.4611 | 123 | 1281 | 139 | 2998 | 1.01 | 2098 | 316 | 0.7662 | 175 | 0.876 |
| METS | 1.4768 | 135 | 1321 | 127 | 2532 | 0.654 | 1011 | 340 | 0.432 | 200 | 0.432 |
| METS | 1.4834 | 147 | 1388 | 139 | 2211 | 0.667 | 1021 | 341 | 0.445 | 219 | 0.411 |
| METS | 1.4911 | 151 | 1411 | 131 | 2019 | 0.713 | 1119 | 356 | 0.449 | 223 | 0.423 |

## INDEPENDENT VARIABLES AS INPUTS:

RI values,T2 value, ADC value ,Quantities of metabolites: ( Choline, Creatine, MI ,NAA, Lipid/ lactate)

Ratio of Choline : NAA, Ratio of Creatine : NAA and Ratio of Cho: Cr.

## DEPENDENT VARIABLE: TO LIVE PREDICT (OUTPUT OR DECISION) :

Diseases like MS, Glioma, Glioblastoma (Grade III/IV Astrocytoma), metastasis and tissues like Gray /white matters, CSF are regarded as dependent variables [17].

Principal Component Analysis: Using XI STAT ( AddinSoft, France) program, PCA (Pearson Type (n) ) was run on the data of the table 1. It contains a matrix of 12 X 31 (12 columns and 31 rows). PCA was applied to analyze and decrease the dimensional representation of ground truth images after extracting several features for output or prediction of diseases. The observations and standard deviation of the variables are tabulated in Table 2.

TABLE 2 Showing observations and standard deviation of the variables:


These features or dependent variables were used as input to PCA which in turn determined the correlation between the variables (Table 3).

In classification process, each training data is converted into a vector. The covariance matrix is computed by multiplying several variance or factors by other factors or variance.

TABLE 3: Correlation of Variables of Matrix

| Correlation matrix (Pearson (n)): |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Variables | ADC | CHO | CR | CH/CR | CHO/NAA | CR/NAA | LIP/LAC | MI | RI | T2 |
|  |  |  |  |  |  |  |  |  |  |  |
| ADC | 1 | 0.023 | 0.178 | 0.296 | -0.113 | -0.703 | -0.085 | 0.062 | -0.485 | 0.623 |
| CHO | -0.023 | 1 | 0.847 | 0.744 | 0.640 | -0.416 | 0.737 | 0.850 | -0.406 | 0.412 |
| CR | -0.178 | 0.847 | 1 | 0.339 | 0.430 | -0.125 | 0.687 | 0.586 | -0.233 | 0.212 |
| CH/CR | 0.296 | 0.744 | 0.339 | 1 | 0.738 | -0.646 | 0.625 | 0.881 | -0.602 | 0.636 |
| CHO/NAA | -0.113 | 0.640 | 0.430 | 0.738 | 1 | -0.041 | 0.733 | 0.753 | -0.243 | 0.219 |
| CR/NAA | -0.703 | 0.416 | 0.125 | -0.646 | -0.041 | 1 | -0.247 | -0.517 | 0.643 | 0.725 |
| LIP/LAC | -0.085 | 0.737 | 0.687 | 0.625 | 0.733 | -0.247 | 1 | 0.872 | -0.454 | 0.415 |
| MI | 0.062 | 0.850 | 0.586 | 0.881 | 0.753 | -0.517 | 0.872 | 1 | -0.551 | 0.542 |
|  |  | - | - |  |  |  |  |  |  |  |
| RI | -0.485 | 0.406 | 0.233 | -0.602 | -0.243 | 0.643 | -0.454 | -0.551 | 1 | 0.974 |
| T2 | 0.623 | 0.412 | 0.212 | 0.636 | 0.219 | -0.725 | 0.415 | 0.542 | -0.974 | 1 |

## RESULT AND DISCUSION

The PCA (Pearson N) analysis provides a good model of these data, with $80 \%$ of the variance explained in the components. Eigenvalues, Variability \% and Cumulative \% in relation to factors were extracted and depicted in the Table4.

Table 4. PRINCIPAL COMPONENT ANALYSIS: showing Eigenvalue, variability and cumulative\%

| Column1 | F1 | F2 | F3 | F4 | F5 | F6 | F7 | F8 | F9 | F10 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Eigenvalue | 5.560 | 2.451 | 0.769 | 0.576 | 0.328 | 0.246 | 0.036 | 0.018 | 0.011 | 0.005 |
| Variability <br> $(\%)$ | 55.596 | 24.514 | 7.693 | 5.763 | 3.281 | 2.457 | 0.357 | 0.181 | 0.112 | 0.046 |
| Cumulative <br> $\%$ | 55.596 | 80.110 | 87.803 | 93.566 | 96.847 | 99.304 | 99.660 | 99.841 | 99.954 | 100.000 |

Eigenvectors of the variables, factors with correlation among the factors were tabulated in the Table 5and 6 respectively.

TABLE 5. EIGENVECTORS:

|  | F1 | F2 | F3 | F4 | F5 | F6 | F7 | F8 | F9 | F10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  | - |
| ADC | 0.124 | 0.532 | 0.031 | 0.297 | 0.707 | 0.094 | 0.247 | 0.078 | 0.022 | 0.188 |
| CHO | 0.363 | 0.226 | 0.258 | 0.297 | 0.078 | 0.352 | 0.313 | 0.125 | 0.647 | 0.008 |
| CR | 0.260 | 0.322 | 0.652 | 0.095 | 0.289 | 0.145 | 0.252 | 0.096 | 0.465 | 0.028 |
| CH/CR | 0.383 | 0.030 | 0.389 | 0.221 | 0.202 | 0.274 | 0.007 | 0.456 | 0.413 | 0.397 |
| CHO/NAA | 0.290 | 0.306 | 0.550 | 0.058 | 0.389 | 0.215 | 0.395 | 0.246 | 0.149 | 0.284 |
| CR/NAA | 0.275 | 0.395 | 0.101 | 0.462 | 0.342 | 0.270 | 0.535 | 0.099 | 0.118 | 0.214 |
| LIP/LAC | 0.346 | 0.256 | 0.019 | 0.246 | 0.161 | 0.716 | 0.052 | 0.401 | 0.177 | 0.141 |
| MI | 0.398 | 0.140 | 0.138 | 0.069 | 0.242 | 0.277 | 0.516 | 0.560 | 0.268 | 0.105 |
| RI | 0.314 | 0.309 | 0.115 | 0.572 | 0.126 | 0.179 | 0.185 | 0.335 | 0.183 | 0.487 |
| T2 | 0.319 | 0.363 | 0.105 | 0.396 | 0.014 | 0.172 | 0.178 | 0.323 | 0.145 | 0.641 |

TABLE6: Correlations between variables and factors

|  | F1 | F2 | F3 | F4 | F5 | F6 | F7 | F8 | F9 | F10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ADC | 0.29 | 0.83 | - | 0.22 |  |  |  |  |  | 0.01 |
|  | 2 | 3 | 0.027 | 6 | 0.405 | 0.047 | 0.047 | 0.011 | 0.002 | 3 |
| CHO | 0.85 | 0.35 |  | 0.22 | - |  |  |  |  | 0.00 |
|  | 6 | 3 | 0.226 | 5 | 0.045 | -0.175 | 0.059 | -0.017 | 0.069 | 1 |
| CR | 0.61 | 0.50 |  | 0.07 |  |  |  |  |  | 0.00 |
|  | 3 | 4 | 0.572 | 2 | 0.166 | -0.072 | -0.048 | 0.013 | -0.049 | 2 |
| CH/CR | 0.90 | 0.04 | - | 0.16 | - |  |  |  |  | 0.02 |
|  | 3 | 7 | 0.341 | 8 | 0.116 | -0.136 | -0.001 | -0.061 | -0.044 | 7 |
| CHO/NA | 0.68 | 0.47 | - | 0.04 |  |  |  |  |  | 0.01 |
| A | 4 | 8 | 0.482 | 4 | 0.223 | -0.106 | -0.075 | 0.033 | 0.016 | 9 |
| CR/NAA | - | - | - | - | 0.196 | -0.134 | 0.101 | -0.013 | -0.012 | - |


|  | $\begin{array}{r} 0.64 \\ 9 \end{array}$ | $\begin{array}{r} 0.61 \\ 8 \end{array}$ | 0.089 | 0.35 0 |  |  |  |  |  | 0.01 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| LIP/LAC |  | - |  | - |  |  |  |  |  | - |
|  | 0.81 | 0.40 |  | 0.18 |  |  |  |  |  | 0.01 |
|  | 6 | 1 | 0.016 | 7 | 0.092 | 0.355 | -0.010 | -0.054 | 0.019 | 0 |
| MI | 0.93 | 0.22 | - | 0.05 | - |  |  |  |  | 0.00 |
|  | 8 | 0 | 0.121 | 2 | 0.139 | 0.137 | 0.097 | 0.075 | -0.028 | 7 |
| RI | 0.74 | 0.48 | - | 0.43 |  |  |  |  |  | 0.03 |
|  | 1 | 4 | 0.101 | 4 | 0.072 | 0.089 | 0.035 | -0.045 | -0.019 | 3 |
|  | 0.75 | 0.56 |  | 0.30 |  |  |  |  |  | 0.04 |
| T2 | 2 | 8 | 0.092 | 1 | 0.008 | -0.085 | 0.034 | -0.043 | -0.015 | 4 |

As the PCA works, normal brain tissue like gray white matter CSF (Cerebro spinal Fluid) and pathological condition like MS, perilesion edema, low grade glioma, high grade glioma, and metastases can be classified or differentiated out of large data.
A scree plot or a simple line segment plot is shown (Figure 2 ) using the fraction of total variance in the data represented by each Principal component or factors fraction explaining the most of cumulative variability and eigenvalues. It represents values in descending order of contribution to total variance.

Scree plot


Figure 2. Scree plot derived prediction of diseases utilizing Eigenvalue, cumulative variability \% and different factors.

The role of PCA is to check the pattern of relationship among the large number of data of the brain tissues and diseases emphasizing their identical nature or disparity, reducing to one dimension.


Figure 3. showing variables ( Parameters) in Axes F1 and F2 (80.11\%) derived from the ground truth images.

By compressing or mapping the data (Figure 3) it converts the large number of dimensions gathered from the ground Truth Image inputs (Table1) into a lower dimensional space. However, the main goal in dimensionality reduction was achieved preserving as much of the significant information as possible.

From the variables shown in Figure 3, a map of the disease or brain tissue can be generated as well (Figure 4). It can be deduced that RI and $\mathrm{Cr} / \mathrm{NAA}$ ratio can discriminate Glioblastoma III/IV, METS, Glioma, Gray/white matters and perilesional edema much better than other variables. On the other hand ADC value can specify CSF. Metabolites like CH:CR.LIP,LAC and

T2 can detect MS clearly away from other lesions.


Figure 4. Variables versus disease and tissue discrimination

Further to Figure 4, PCA could extract maps (Figure 5 and 6) of brain tissue and diseases (lesions) from the observations (variables), separating each entity in the space representing F1 and F2 dimension. Glioblastoma Gr II/IV and metastases stand out in the periphery away from the normal tissue of gray and white matters, CSF. Glioma and a fraction MS are placed close to gray/white matters. However Gr I and II Glioblastoma lies in the vicinity of the low grade Glioma.


Figure 5. Mapping of the normal brain tissues and lesions by PCA utilizing observations F1 and $\mathrm{F} 2 \mathbf{( 8 0 . 1 1 \%}$ ) are shown.

Conclusion: PCA an important statistical device can reduce the number and dimension of complex variables like the parameters extracted from the ground truth MR images and produce a linear relationship in a simple way. Mapping of tissue and diseases can be generated from the depleted variables loosing their complex dimensionality.

Thus PCA helps discriminating different disease process and brain tumors. RI is found to be superior to all other parameters (like T2 values, ADC values and important metabolites and their ratio) in differentiating diseases.

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